## Dividing Fractions ANSWERS

Section A Reciprocals

1) Prove that $\frac{3}{4} \times \frac{4}{3}=1$

$$
\frac{3}{4} \times \frac{4}{3}=\frac{12}{12}=1
$$

2) Fill in the blanks:
a) $\frac{2}{3} \times \frac{3}{2}=1$
b) $\frac{7}{5} \times \frac{5}{7}=1$
c) $1=\frac{1}{2} \times 2$
d) $\frac{1}{8} \times 8=1$

## Any number multiplied by

 its reciprocal is equal to 1.3) Find the reciprocal of each of the following numbers:
a) $\frac{6}{11} \frac{11}{6}$
b) $-\frac{2}{3}-\frac{3}{2}$
c) $5 \frac{1}{5}$
d) $\frac{1}{2} 2$
e) $\frac{8}{19} \quad \frac{19}{8}$
f) $4 \frac{2}{3} \quad \frac{3}{14}$

Section B Dividing integers by fractions
1)

| 1 |  |  |
| :---: | :---: | :---: |
| $\frac{1}{3}$ | $\frac{1}{3}$ | $\frac{1}{3}$ |

Explain how this diagram shows that $1 \div \frac{1}{3}=3$.
$1 \div \frac{1}{3}$ means how many $\frac{1}{3}$ 's are in 1 .
The diagram shows that there are 3 lots of $\frac{1}{3}$ in 1 .
2) Calculate the following:
a) $2 \div \frac{1}{3}=6$
b) $2 \div \frac{2}{3}=3$
c) $10 \div \frac{2}{3}=30$
d) $10 \div \frac{2}{5}=25$
e) $10 \div \frac{3}{5}=16 \frac{2}{3}$
f) $21 \div 2 \frac{1}{3}=9$

Section C Dividing any pair of fractions

1) Calculate:
a) $\frac{1}{3} \div \frac{1}{3}=\frac{3}{2}$
b) $\frac{2}{3} \div \frac{1}{2}=\frac{4}{3}$
c) $4 \frac{2}{3} \div \frac{1}{2}=9 \frac{1}{3}$
d) $\frac{5}{7} \div \frac{5}{12}=1 \frac{5}{7}$
e) $-\frac{5}{12} \div \frac{4}{9}=-\frac{15}{16}$
f) $2 \frac{1}{8} \div \frac{9}{10}=2 \frac{13}{36}$
g) $\frac{9}{11} \div \frac{9}{11}=1$
h) $\frac{7}{12} \div \frac{3}{4} \div \frac{1}{2}=1 \frac{5}{9}$
i) $3 \frac{1}{7} \div 5 \frac{1}{2}=\frac{4}{7}$

Section D Identify and explain the mistake:

$$
\text { 1) } \begin{aligned}
\frac{6}{20} \div \frac{4}{3} & =\frac{20}{6} \times \frac{4}{3} \\
& =\frac{80}{18} \\
& =4 \frac{4}{9}
\end{aligned}
$$

The reciprocal of both fractions has been multiplied.
The correct calculation is $\frac{6}{20} \times \frac{3}{4}$.
2) $\frac{3}{8} \div 4=\frac{3}{8} \times \frac{4}{1}$

$$
=\frac{12}{8}
$$

$$
=1 \frac{1}{2}
$$

The reciprocal of 4 is $\frac{1}{4}$ so dividing by 4 is the same as multiplying by $\frac{1}{4}$.
The correct calculation is $\frac{3}{8} \times \frac{1}{4}=\frac{3}{32}$.

Section $\boldsymbol{E}$ Simplify the following:

| a) $\frac{a}{b} \div \frac{c}{d}=\frac{a d}{b c}$ | d) $a \div \frac{b}{c}=\frac{a c}{b}$ | g) $\frac{2 a}{b} \div \frac{2 a^{2}}{7 b}=\frac{7}{a}$ |
| :--- | :--- | :--- |
| b) $\frac{a}{b} \div \frac{a}{c}=\frac{c}{b}$ | e) $\frac{a}{b} \div c=\frac{a}{b c}$ | h) $\frac{a}{2} \div \frac{a}{2}=1$ |
| c) $\frac{a}{7} \div \frac{2}{a}=\frac{a^{2}}{14}$ | f) $\frac{2 a}{b} \div \frac{c}{7 b}=\frac{14 a}{c}$ | i) $\frac{(x+1)}{7} \div \frac{(x+2)}{3}=\frac{3(x+1)}{7(x+2)}$ |

Section $\boldsymbol{F} \quad$ Complete each puzzle below:

1) Use each of the following numbers to make the calculations correct.

2) Fill the gaps in the multiplication grid.

| $x$ | $\frac{1}{2}$ | $\frac{1}{6}$ | $\frac{8}{15}$ |
| :---: | :---: | :---: | :---: |
| 8 | 4 | $\frac{4}{3}$ | $4 \frac{4}{15}$ |
| 6 | 3 | 1 | $3 \frac{1}{5}$ |
| 5 | $2 \frac{1}{2}$ | $\frac{5}{6}$ | $2 \frac{2}{3}$ |

